

## Atomic arrangement of $\delta$ - $\text{Bi}_2\text{O}_3$ with defective fluorite structure by first-principles calculations

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$\text{Bi}_2\text{O}_3$  forms a monoclinic phase ( $\alpha$ - $\text{Bi}_2\text{O}_3$ ) at room temperature, and transforms into a cubic phase ( $\delta$ - $\text{Bi}_2\text{O}_3$ ) at about 1000 K [1, 2].  $\delta$ - $\text{Bi}_2\text{O}_3$  exhibits high oxide-ion conduction, while  $\alpha$ - $\text{Bi}_2\text{O}_3$  does not [3]. Hence, the atomic structure of  $\delta$ - $\text{Bi}_2\text{O}_3$ , especially its relationship with the ionic conduction, is interesting. The framework of  $\delta$ - $\text{Bi}_2\text{O}_3$  is the fluorite structure. Since the ratio of Bi atoms to oxygen is 2 to 3, a quarter of the oxygen sites is vacant for charge neutrality. The arrangement of the occupied and vacant sites on the oxygen sublattice has been reported as disordered [4, 5]. However, local structures of  $\delta$ - $\text{Bi}_2\text{O}_3$  have been left open, although they are essential information to discuss the origin of the ionic conduction.

The difficulty in treating  $\delta$ - $\text{Bi}_2\text{O}_3$  by first-principles calculations resides in the disordered arrangement of oxygen site vacancies. In the present study, we have examined many structural models with different arrangements of oxygen site vacancies. First-principles calculations within the generalized gradient approximation were made using the plane-wave basis projector-augmented wave method as implemented in the VASP code [6].

We first examine the defective structure within the unit cell of the fluorite (10 atoms). There are only 3 independent arrangements with the vacant sites ordered in  $\langle 001 \rangle$ ,  $\langle 011 \rangle$ , and  $\langle 111 \rangle$  directions, respectively. We hereafter call them 001-, 011- and 111-model, respectively. They have high symmetry if oxygen atoms are set at the ideal positions of the fluorite structure. However, when a small displacement is introduced for every atom to break the symmetry, their total energies are significantly decreased. For instance, the 111-model shows lower energy by 1.4 eV/formula-unit by the breaking of the symmetry. In order to overcome the restriction of the small cell, a set of larger supercells (80 atoms,  $2 \times 2 \times 2$  expansion of the unit cell) is examined. In addition, calculations of  $\text{Y}_2\text{O}_3$  using the same set of models are made. Similar to some other rare-earth oxides,  $\text{Y}_2\text{O}_3$  is known to form the bixbyite structure under ordinary conditions. The bixbyite structure is composed of octants that are identical to the 111-model of the defective fluorite structure as shown in Fig. 1. It can therefore be included in the 80-atom cell examined in the present study.

Figure 2 shows relative energies of different models for both  $\delta$ - $\text{Bi}_2\text{O}_3$  and  $\text{Y}_2\text{O}_3$ . Energies of four corresponding structures are connected by dotted lines. Both of  $\delta$ - $\text{Bi}_2\text{O}_3$  and  $\text{Y}_2\text{O}_3$  show the lowest energy with the bixbyite structure. In  $\delta$ - $\text{Bi}_2\text{O}_3$ , the 001-model also shows the lowest energy. As can be seen in Fig. 2,  $\delta$ - $\text{Bi}_2\text{O}_3$  shows much smaller variation in energy than  $\text{Y}_2\text{O}_3$  among different models. This should be related to the significant disordering of the oxygen site vacancies in  $\delta$ - $\text{Bi}_2\text{O}_3$ . At high temperatures, configurational entropy contribution overcomes the small internal energy differences among different local structures, leading to the stabilization of the disordered structures.

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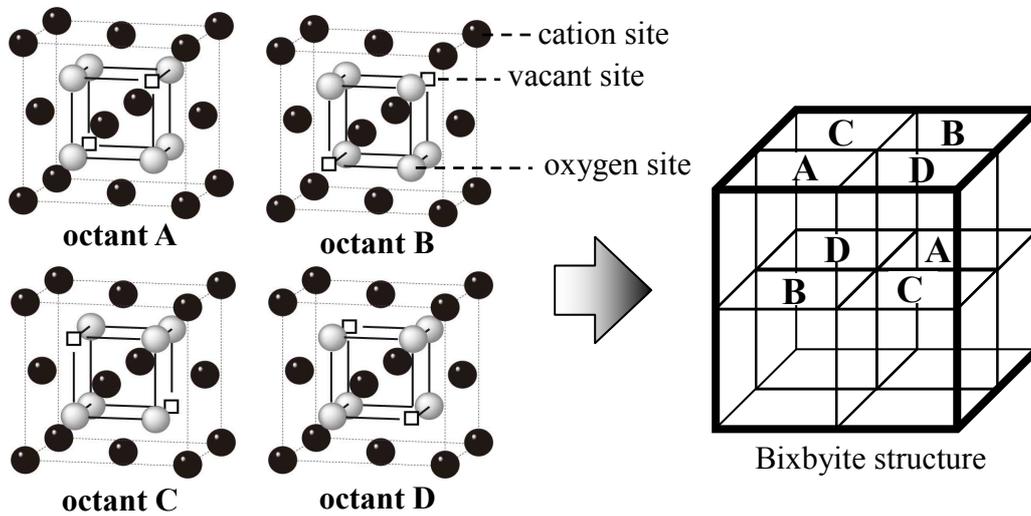


Fig. 1. The construction of the bixbyite structure by octants that are identical to the 111-model of the defective fluorite structure. Black, light-gray spheres and white square denote cation, oxygen, and vacant sites, respectively.

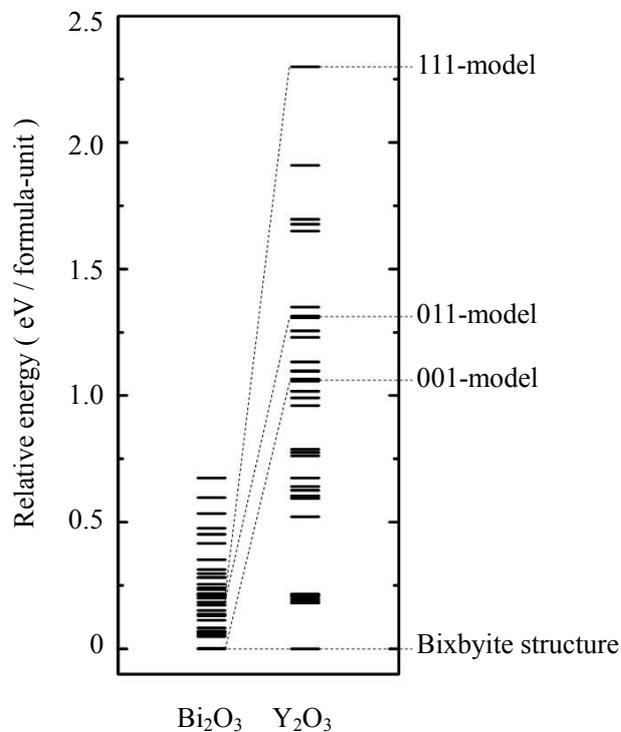


Fig. 2. Relative energies of a set of different models for  $\delta$ - $\text{Bi}_2\text{O}_3$  and  $\text{Y}_2\text{O}_3$  within the defective fluorite structure composed of 80 atoms.